New Developments in Parton Showers


Work in collaboration with W. Giele, D. Kosower, J. Lopez-Villarejo,
A. Gehrmann-de-Ridder, M. Ritzmann, E. Laenen, L. Hartgring

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P. Skands



[^0]
## New Developments in Parton Showers

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[^1]
## "New" ?

## For matching to the first emission:

$=$ PYTH|A scheme Sjöstrand \& Bengtsson, PLB 185 (I987) 435, NPB 289 (1987) 810 (reformulated for antennae)

## For matching to the first loop:

$=$ POWHEG Scheme Nason, JHEP 04II (2004) 040; Nason, Ridolfi, JHEP 0608 (2006) 077;
(real-emission part same as PYTHIA, hence compatible)
What is new (apart from antennae):
Repeating this for the next emission, and the next, ...
GKS ~ multileg scheme (unitary) that reduces to PYTHIA/POWHEG at $\left.\right|^{\text {st }}$ order
Unitarity $\rightarrow$ No "matching scale" needed
Faster than MLM, CKKW (no initialization, no separate n-parton phase-spaces)
Calculation also yields $\sim 10$ automatic uncertainty estimates at a moderate speed penalty

## $1^{\text {st }}$ Order: PYTHIA and POWHEG

## PYTHIA

FSR: Sjöstrand \& Bengtsson, PLBI85(I987)435, NPB289(I987)8IO
Drell-Yan: Miu \& Sjöstrand, PLB449(I999)3I3

## Real Radiation:

$$
\left.\frac{\mathrm{d} \hat{\sigma}}{\mathrm{~d} \hat{t}}\right|_{\mathrm{PS}}=\left.\frac{\mathrm{d} \hat{\sigma}}{\mathrm{~d} \hat{t}}\right|_{\mathrm{PS} 1}+\left.\frac{\mathrm{d} \hat{\sigma}}{\mathrm{~d} \hat{t}}\right|_{\mathrm{PS} 2}=\frac{\sigma_{0}}{\hat{s}} \frac{\alpha_{\mathrm{s}}}{2 \pi} \frac{4}{3} \frac{\hat{s}^{2}+m_{\mathrm{W}}^{4}}{\substack{\mathrm{~W} \\ \mathrm{q}_{\left.\mathrm{q} g \rightarrow \mathrm{q}^{\prime} \mathrm{W}\right)}}}
$$

Use PS as overestimate. Correct to $R / B$ via veto:

$$
\begin{aligned}
& R_{\mathrm{qg} \rightarrow \mathrm{q}^{\prime} \mathrm{W}}(\hat{s}, \hat{t}) \underset{\text { (+analogous for } \mathrm{qq} \rightarrow \mathrm{gW})}{=} \frac{(\mathrm{d} \hat{\sigma} / \mathrm{d} \hat{t})_{\mathrm{ME}}}{(\mathrm{~d} \hat{\sigma} / \mathrm{d} \hat{t})_{\mathrm{PS}}}=\frac{\hat{s}^{2}+\hat{u}^{2}+2 m_{\mathrm{W}}^{2} \hat{t}}{\hat{s}^{2}+2 m_{\mathrm{W}}^{2}(\hat{t}+\hat{u})} \\
& \text { Unitarity } \rightarrow \text { Modified Sudakov Factor: } \\
& \exp \left(-\int_{t}^{t_{\max }} \mathrm{d} t^{\prime} \frac{\alpha_{\mathrm{s}}\left(t^{\prime}\right)}{2 \pi} \sum_{a} \int_{x}^{1} \mathrm{~d} z \frac{x^{\prime} f_{a}\left(x^{\prime}, t^{\prime}\right)}{x f_{b}\left(x, t^{\prime}\right)} P_{a \rightarrow b c}(z)\right)
\end{aligned}
$$

Inclusive Cross Section (at fixed underlying Born variables):

$$
\begin{aligned}
& \text { Unitarity + no normalization correction } \rightarrow \text { remains } \sigma_{0} \\
& \rightarrow B=\sigma_{0}=\left|M_{\text {Born }}\right|^{2}
\end{aligned}
$$

Cancels when normalizing to $1 / \sigma$ and integrating over Born

Note: $\rightarrow$ tuning of standalone PYTHIA done with this matching scheme
Should be OK for POWHEG, but could give worries for MLM B. Cooper et al, arXiv: I I 09.5295

## $1^{\text {st }}$ Order: PYTHIA and POWHEG

PYTHIA
FSR: Sjöstrand \& Bengtsson, PLBI85(1987)435, NPB289(1987)8।0 Drell-Yan: Miu \& Sjöstrand, PLB449(1999)3।3

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$$

Use PS as overestimate. Correct to $R / B$ via veto:

$$
\begin{aligned}
& \underset{\substack{\left.\mathrm{gq} \rightarrow \mathrm{q}^{\prime} \mathrm{W}(\hat{s}, \hat{t}) \\
\text { (analogous for qq } \rightarrow \mathrm{gW}\right)}}{R_{\text {a }}}=\frac{(\mathrm{d} \hat{\sigma} / \mathrm{d} \hat{t})_{\mathrm{ME}}}{(\mathrm{~d} \hat{\sigma} / \mathrm{d})_{\mathrm{PS}}}=\frac{\hat{s}^{2}+\hat{u}^{2}+2 m_{\mathrm{W}}^{2} \hat{t}}{\hat{s}^{2}+2 m_{\mathrm{W}}^{2}(\hat{t}+\hat{u})} \\
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POWHEG
Nason, JHEP II(2004)040
Drell-Yan: Alioli et al., JHEP 07(2008)060

## Real Radiation:

$$
R_{g \bar{q}, q}+R_{q g, \bar{q}}=\left.\frac{\mathrm{d} \hat{\sigma}}{\mathrm{~d} \hat{t}}\right|_{\mathrm{ME}}=\frac{\sigma_{0}}{\hat{s}} \frac{\alpha_{\mathrm{s}}}{2 \pi} \frac{4}{3} \frac{t^{2}+\hat{u}^{2}+2 m_{\mathrm{W}}^{2} \hat{s}}{\text { (using Sjöstrand's notation) }} \frac{\hat{q^{\prime}} \hat{\mathrm{W}}}{}
$$

Use $R / B$ as splitting kernels (via overestimate + veto)
(+analogous for $\mathrm{qq} \rightarrow \mathrm{gW}$ )

## Unitarity $\rightarrow$ Sudakov Factor:

(explicit formula only for final-state in org paper $\rightarrow$ no PDF factors here)

$$
\begin{array}{cc}
\Delta_{R}^{(\mathrm{NLO})}\left(p_{\mathrm{T}}\right)=e^{-\int d \Phi_{r} \frac{R(v, r)}{B(v)} \theta\left(k_{\mathrm{T}}(v, r)-p_{\mathrm{T}}\right)} \\
\quad \begin{array}{c}
\text { (not needed if shower ordered in } \mathrm{LT}, \\
\text { though watch out, see next) }
\end{array}
\end{array}
$$

Inclusive Cross Section (at fixed underlying Born variables): Include correction to NLO inclusive level $\rightarrow$ becomes $\sigma_{N L O}$

$$
\begin{aligned}
\rightarrow \quad \bar{B}(v) & =B(v)+V(v) \\
& +\int(R(v, r)-C(v, r)) d \Phi_{r}
\end{aligned}
$$

Cancels when normalizing to $1 / \sigma$ and integrating over Born

## Differences?

Standard Les Houches interface (LHA, LHEF) specifies startup scale SCALUP for showers, so "trivial" to interface any external program, including POWHEG.
Problem: for ISR

$$
p_{\perp}^{2}=\mathrm{p}_{\perp \mathrm{evol}}^{2}-\frac{\mathrm{p}_{\perp \mathrm{evol}}^{4}}{p_{\perp \mathrm{evol}, \mathrm{max}}^{2}}
$$

$$
\int d \Phi_{r} \frac{R(v, r)}{B(v)} \theta\left(k_{\mathrm{T}}(v, r)-p_{\mathrm{T}}\right)
$$

not needed if shower ordered in PT ?
i.e. $p_{\perp}$ decreases for $\theta^{*}>90^{\circ}$ but $\mathrm{p}_{\perp \text { evol }}$ monotonously increasing. Solution: run "power" shower but kill emissions above the hardest one, by POWHEG's definition.
(a)

(b)


Available, for ISR-dominated, coming for QCD jets with FSR issues.

## VINCIA

## What is it?

Plug-in to PYTHIA 8 http://projects.hepforge.org/vincia

## What does it do?



The VINCIA Code
"Matched Markov antenna showers"
Improved parton showers

+ Re-interprets tree-level matrix elements as $2 \rightarrow \mathrm{n}$ antenna functions
+ Extends matching to soft region (no "matching scale")
Automated uncertainty estimates
Systematic variations of shower functions, evolution variables, $\mu_{R}$, etc.
$\rightarrow$ A vector of output weights for each event (central value $=$ unity $=$ unweighted)


## Who is doing it?

GEEKS: Giele, Kosower, PS

+ Collaborations with Sjostrand (Pythia 8 interface), Gehrmann-de-Ridder \& Ritzmann (mass effects),
Lopez-Villarejo \& Larkoski (sector showers, helicity-dependence), Hartgring \& Laenen (NLL/NLO multileg),
Diana (ISR), Volunteers (Tuning)


## Markov pQCD

Start at Born level
$\left|M_{F}\right|^{2}$


## Markov pQCD

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$$
\left|M_{F}\right|^{2}
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Generate "shower" emission

$$
\left|M_{F+1}\right|^{2} \stackrel{L L}{\sim} \sum_{i \in \mathrm{ant}} a_{i}\left|M_{F}\right|^{2}
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Correct to Matrix Element

$$
\stackrel{\text { PYTHHA trick }}{a_{i}} \frac{\left|M_{F+1}\right|^{2}}{\sum a_{i}\left|M_{F}\right|^{2}}
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\stackrel{\text { PYTHIAA trick }}{ } a_{i} \xrightarrow[\left|M_{F+1}\right|^{2}]{\sum a_{i}\left|M_{F}\right|^{2}}
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Unitarity of Shower
Virtual $=-\int$ Real

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## Unitarity of Shower

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Correct to Matrix Element
$\left|M_{F}\right|^{2} \rightarrow\left|M_{F}\right|^{2}+2 \operatorname{Re}\left[M_{F}^{1} M_{F}^{0}\right]+\int$ Real

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## The Denominator

## In a traditional parton shower, you would face the following problem:

Existing parton showers are not really Markov Chains
Further evolution (restart scale) depends on which branching happened last
$\rightarrow$ proliferation of terms
Number of histories contributing to $\mathrm{n}^{\text {th }}$ branching $\propto \mathbf{2}^{\mathbf{n}} \mathbf{n}$ !

$$
\begin{aligned}
& E \sim K+K+K+M, \begin{array}{l}
i=2 \\
\rightarrow 4 \text { terms }
\end{array} \\
& (K \sim \pi+K) \substack{i=1 \\
\rightarrow 2 \text { terms }} \substack{i}
\end{aligned}
$$

(+ parton showers have complicated and/or frame-dependent phase-space mappings, especially at the multi-parton level)

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$$

Parton- (or Catani-Seymour) Shower:
After 2 branchings: 8 terms
After 3 branchings: 48 terms After 4 branchings: 384 terms
(+ parton showers have complicated and/or frame-dependent phase-space mappings, especially at the multi-parton level)

## Matched Markovian Antenna Showers

Antenna showers: one term per parton pair
$\mathbf{2}^{\mathrm{n}} \mathrm{n}!\rightarrow \mathrm{n}$ !

(+ generic Lorentz-
invariant and on-shell phase-space factorization)

+ Change "shower restart" to Markov criterion:
Given an n-parton configuration,"ordering" scale is

$$
Q_{\text {ord }}=\min \left(Q_{E I}, Q_{E 2}, \ldots, Q_{E n}\right)
$$

Unique restart scale, independently of how it was produced

+ Matching: $\mathrm{n}!\rightarrow \mathbf{n}$
Given an $n$-parton configuration, its phase space weight is:
$\left|M_{n}\right|^{2}$ : Unique weight, independently of how it was produced


## Matched Markovian Antenna Showers

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Matched Markovian Antenna Shower:
After 2 branchings: 2 terms
After 3 branchings: 3 terms
After 4 branchings: 4 terms

Parton- (or Catani-Seymour) Shower:
After 2 branchings: 8 terms
After 3 branchings: 48 terms After 4 branchings: 384 terms

[^2]
## Approximations

## Distribution of Logıo(PSLo/MELo) (inverse ~ matching coefficient)

Dead Zone: I-2\% of phase space have no strongly ordered paths leading there*
*fine from strict LL point of view: those points correspond to "unordered" non-log-enhanced configurations

## $\rightarrow$ Better Approximations

## Distribution of Logı(PSLo/MELo) (inverse ~ matching coefficient)



Leading Order, Leading Color, Flat phase-space scan, over all of phase space (no matching scale)


## $2 \rightarrow 4$

## Generate Trials without imposing strong ordering

At each step, each dipole allowed to fill its entire phase space Overcounting removed by matching

+ smooth ordering beyond matched multiplicities

$$
\frac{\hat{p}_{\perp}^{2}}{\hat{p}_{\perp}^{2}+p_{\perp}^{2}} P_{\mathrm{LL}} \quad \begin{array}{ll}
\hat{p}_{\perp}^{2} & \text { last branching } \\
p_{\perp}^{2} & \text { current branching }
\end{array}
$$




## $2 \rightarrow 4$

## Generate Trials without imposing strong ordering

At each step, each dipole allowed to fill its entire phase space Overcounting removed by matching

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\hat{p}_{\perp}^{2} & \text { last branching } \\
p_{\perp}^{2} & \text { current branching }
\end{array}
$$




## + Matching (+ full colour)


$\rightarrow$ A very good all-orders starting point


# Uncertainties 

## Uncertainty Variations

## A result is only as good as its uncertainty

Normal procedure:
Run MC $2 \mathrm{~N}+$ I times (for central +N up/down variations)
Takes $2 \mathrm{~N}+\mathrm{I}$ times as long

+ uncorrelated statistical fluctuations


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Normal procedure:
Run MC 2N+I times (for central + N up/down variations)
Takes $2 \mathrm{~N}+\mathrm{I}$ times as long

+ uncorrelated statistical fluctuations


## Automate and do everything in one run

VINCIA: all events have weight = I
Compute unitary alternative weights on the fly
$\rightarrow$ sets of alternative weights representing variations (all with $<w\rangle=I$ ) Same events, so only have to be hadronized/detector-simulated ONCE!

MC with Automatic Uncertainty Bands

## Uncertainties

For each branching, recompute weight for:

- Different renormalization scales
- Different antenna functions
- Different ordering criteria
- Different subleading-color treatments

|  | Weight |
| :--- | :---: |
| Nominal | I |
| Variation | $P_{2}=\frac{\alpha_{s 2} a_{2}}{\alpha_{s 1} a_{1}} P_{1}$ |

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## + Unitarity

For each failed branching:

$$
P_{2 ; \mathrm{no}}=1-P_{2}=1-\frac{\alpha_{s 2} a_{2}}{\alpha_{s 1} a_{1}} P_{1}
$$

## Uncertainties

## For each branching, recompute weight for:

- Different renormalization scales
- Different antenna functions
- Different ordering criteria
- Different subleading-color treatments


## + Matching

Differences explicitly matched out
(Up to matched orders)
(Can in principle also include variations of matching scheme...)

|  | Weight |
| :--- | :---: |
| Nominal | I |
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## + Unitarity

For each failed branching:

$$
P_{2 ; \mathrm{no}}=1-P_{2}=1-\frac{\alpha_{s 2} a_{2}}{\alpha_{s 1} a_{1}} P_{1}
$$

## Automatic Uncertainties

## Vincia:uncertaintyBands = on



Variation of renormalization scale (no matching)

## Automatic Uncertainties

## Vincia:uncertaintyBands = on



Variation of "finite terms" (no matching)

## Putting it Together

VinciaMatching:order $=0$
VinciaMatching:order $=3$



## SECTOR SHOWERS

J. Lopez-Villarejo \& PS, arXiv:I 109.3608

Also discussed in Larkoski \& Peskin, PRD8I(2010)0540 IO, PRD84 (201 I)034034

## - Dipole-antenna formalism (2 -> 3)



# SECTOR SHOWERS 

## - Dipole-antenna formalism (2 -> 3)

Lund, GGG, GKS


-.-.......- *)shows Global without any ordering condition imposed $\rightarrow$ overcounting

# NUMBER OF TERMS 

## Global FSR shower (default VINCIA)

|  | "Traditional" <br> parton shower | Vincia Markov global <br> antenna shower | Vincia Markov sector <br> antenna shower |
| :---: | :---: | :---: | :---: |
| \# of terms <br> produced in the <br> shower | $2^{\mathrm{N}} \mathrm{N}!$ | N | 1 |

$\mathrm{N}=$ number of emitted partons
2 terms per phase-space point

## NUMBER OF TERMS

## $\rightarrow$ Sector shower

|  | "Traditional" <br> parton shower | Vincia Markov global <br> antenna shower | Vincia Markov sector <br> antenna shower |
| :---: | :---: | :---: | :---: |
| \# of terms <br> produced in the <br> shower | $2^{\mathrm{N} N!}$ | N | 1 |

$\mathrm{N}=$ number of emitted partons

## SECTOR IMPLEMENTATION

- Implementation based on the global shower setup.
- Antenna functions are different than in the global case. $\rightarrow$ Challenges (partitioning of collinear radiation singularities)
- Different criteria for separating sectors in phase space Looking for "best" sub-LL behavior.



## RESULTS->FF

## Test: fragmentation function for a quark



## RESULTS -> SPEGD

| Matched through: | $\mathrm{Z} \rightarrow 3$ | $\mathrm{Z} \rightarrow 4$ | $Z \rightarrow 5$ | $\mathrm{Z} \rightarrow 6$ |
| :---: | :---: | :---: | :---: | :---: |
| Pythia 6 | 0.20 | ms/event <br> $\mathrm{Z} \rightarrow \mathrm{qq}(\mathrm{q}=u d s c b)+$ shower. Matched and unweighted. Hadronization of gfortran/g++ with gec v.4.4-O2 on single 3.06 GHz processor with 4GB memory |  |  |
| Pythia 8 | 0.22 |  |  |  |
| Vincia Global | 0.30 | 0.77 | 6.40 | 130.00 |
| Vincia Sector | 0.27 | 0.63 | 6.90 | 52.00 |
| Vincia Global ( $\mathrm{Qmatch}=5 \mathrm{GeV}$ ) | 0.29 | 0.60 | 2.40 | 20.00 |
| Vincia Sector ( $\mathrm{Qmach}=5 \mathrm{GeV}$ ) | 0.26 | 0.50 | 1.40 | 6.70 |
| Sherpa ( $\left.\mathrm{Q}_{\text {match }}=5 \mathrm{GeV}\right)$ | 5.15* | 53.00* | 220.00* | 400.00* |
| * + initialization time | 1.5 minutes | 7 minutes | 22 minutes | 2.2 hours |

Generator Versions: Pythia 6.425 (Perugia 2011 tune), Pythia 8.I50, Sherpa 1.3.0, Vincia 1.026 (without uncertainty bands, NLL/NLC=OFF)

VINCIA STATUS
PLUG-IN TO PYTHIA 8
STABLE AND RELIABLE FOR FINAL-
STATE JETS (Eg. Iep)
AUTOMATIC MATCHING AND
UNCERTAINTY BANDS
IMPROVEMENTS IN SHOWER
(SMOOTH ORDERING, NLC, MATCHING, ...)
PAPER ON MASS EFFECTS~READY
(WITH A. GEHRMANN-DE-RIDDER \& M. RITZMANN)
NEXT STEPS
MULTI-LEG ONE-LOOP MATCHING
(WITH L. HARTGRING \& E. LAENEN, NIKHEF)
POLARIZED SHOWERS
(WITH A. LARKOSKI, SLAC, \& J. LOPEZ-VILLAREJO, CERN)
$\rightarrow$ INITIAL-STATE SHOWERS
(With W. Giele, D. Kosower, G. Diana, M. Ritzmann)

VINCIA STATUS
Hoviver
\#1 GUEST RATED SHOWERHEAD - ALL NEW

NEXT STEPS
MULTI-LEG ONE-LOOP MATCHING
(WITH L. HARTGRING \& E. LAENEN, NIKHEF)
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$\qquad$


## Simple Solution

## Generate Trials without imposing strong ordering

At each step, each dipole allowed to fill its entire phase space
Overcounting removed by matching
(revert to strong ordering beyond matched multiplicities)



## (Subleading Singularities)

## Isolate double-collinear region: $\alpha_{3}^{2 l^{2}}$



## LEP event shapes





## PYTHIA 8 already doing a very good job

## VINCIA adds uncertainty bands + can look at more exclusive observables?

## Multijet resolution scales




## 4-Jet Angles

## 4-jet angles

## Sensitive to

 polarization effects
## Good News

VINCIA is doing reliably well
Non-trivial verification that shower+matching is working, etc.

## Higher-order matching needed?

PYTHIA 8 already doing a very good job on these observables




Interesting to look at more exclusive observables, but which ones?


[^0]:    Work in collaboration with W. Giele, D. Kosower, J. Lopez-Villarejo,
    A. Gehrmann-de-Ridder, M. Ritzmann, E. Laenen, L. Hartgring

[^1]:    Work in collaboration with W. Giele, D. Kosower, J. Lopez-Villarejo,
    A. Gehrmann-de-Ridder, M. Ritzmann, E. Laenen, L. Hartgring

[^2]:    +J . Lopez-Villarejo $\rightarrow$ I term at any order

