Photo-nuclear collisions in PYTHIA 8

UPC 2023: INTERNATIONAL WORKSHOP ON THE PHYSICS OF ULTRA PERIPHERAL COLLISIONS



Motivation: data for inclusive γ -p and γ -Pb from UPCs at the LHC



• Multiplicity distribution well in line for γ -p but γ -p not enough for γ -Pb

Motivation: data for inclusive $\gamma\text{-}\mathrm{p}$ and $\gamma\text{-}\mathrm{Pb}$ from UPCs at the LHC



- Multiplicity distribution well in line for γ -p but γ -p not enough for γ -Pb
- · CMS γ -p v_2 reproduced with Pythia, ATLAS data show finite v_2 and v_3 in γ -Pb

Outline

PYTHIA 8: A general purpose event generator

- Latest release 8.310 (July 2023)
- A new physics manual for 8.3

[SciPost Phys. Codebases 8-r8.3 (2022)]

Outline

- 1. Pythia 8 basics
- 2. Photoproduction in e+p at HERA
- 3. UPCs at the LHC
 - Photon fluxes in Pythia
 - Photon-ion collisions
 - v₂ extraction
- 4. Summary & Outlook



[figure by P. Skands]

Physics modelled within Рүтніа 8

Classify event generation in terms of "hardness"

1. Hard Process (here $t\bar{t}$)



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- 2. Resonance decays (t, Z, ...)



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- Matching, Merging and matrix-element corrections



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 - ISR, FSR, QED, Weak



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- 6. Hadronization, Beam remnants
- 7. Decays, Rescattering



Photoproduction in HERA

Electron-proton collisions and connection to UPCs

Classified in terms photon virtuality Q^2

Deep inelastic scattering (DIS)

- High virtuality, $Q^2 > a$ few GeV²
- Lepton scatters off a parton by exchanging a highly virtual photon

Photoproduction (PhP)

- Low virtuality, $Q^2
 ightarrow 0~{
 m GeV^2}$
 - \Rightarrow Similar to UPCs
- Photon may fluctuate into a hadronic state, resolved in the interaction
- Hard scale μ provided by the final state



Photon structure at $Q^2 \approx 0 \text{ GeV}^2$



Partonic structure of resolved (anom. + VMD) photon encoded in photon PDFs

$$f_i^{\gamma}(\mathbf{x}_{\gamma}, \mu^2) = f_i^{\gamma, \text{dir}}(\mathbf{x}_{\gamma}, \mu^2) + f_i^{\gamma, \text{anom}}(\mathbf{x}_{\gamma}, \mu^2) + f_i^{\gamma, \text{VMD}}(\mathbf{x}_{\gamma}, \mu^2)$$

•
$$f_i^{\gamma,\text{dir}}(x_\gamma,\mu^2) = \delta_{i\gamma}\delta(1-x_\gamma)$$

- $f_i^{\gamma,\text{anom}}(x_{\gamma},\mu^2)$: Perturbatively calculable
- $f_i^{\gamma,\text{VMD}}(x_{\gamma},\mu^2)$: Non-perturbative, fitted or vector-meson dominance (VMD)

Factorized cross section

$$\mathrm{d}\sigma^{\mathrm{b}\mathrm{p}\to\mathrm{k}l+X} = f^{\mathrm{b}}_{\gamma}(\mathrm{x})\otimes f^{\gamma}_{j}(\mathrm{x}_{\gamma},\mu^{2})\otimes f^{\mathrm{p}}_{i}(\mathrm{x}_{\mathrm{p}},\mu^{2})\otimes \mathrm{d}\sigma^{ij\to\mathrm{k}l}$$

ISR probability based on DGLAP evolution

· Add a term corresponding to $\gamma \rightarrow q\overline{q}$ to (conditional) ISR probability

$$\mathrm{d}\mathcal{P}_{a\leftarrow b} = \frac{\mathrm{d}Q^2}{Q^2} \frac{\alpha_{\rm s}}{2\pi} \frac{x' f_a^{\gamma}(x',Q^2)}{x f_b^{\gamma}(x,Q^2)} P_{a\rightarrow bc}(z) \,\mathrm{d}z + \frac{\mathrm{d}Q^2}{Q^2} \frac{\alpha_{\rm em}}{2\pi} \frac{e_b^2 P_{\gamma\rightarrow bc}(x)}{f_b^{\gamma}(x,Q^2)}$$

- \cdot Corresponds to ending up to the beam photon during evolution
 - \Rightarrow Parton originated from the point-like (anomalous) part of the PDFs
 - No further ISR or MPIs below the scale of the splitting
 - Implemented only for Simple Shower in PYTHIA



Comparison to HERA dijet photoproduction data

ZEUS dijet measurement

- $Q^2 < 1.0 \text{ GeV}^2$
- 134 $< W_{\gamma \mathrm{p}} <$ 277 GeV
- + $E_{\rm T}^{\rm jet1}$ > 14 GeV, $E_{\rm T}^{\rm jet2}$ > 11 GeV
- $-1 < \eta^{\text{jet1,2}} < 2.4$

Two contributions

- Momentum fraction of partons in photon $x_{\gamma}^{\text{obs}} = \frac{E_{\text{T}}^{\text{jet1}}e^{\eta^{\text{jet1}}} + E_{\text{T}}^{\text{jet2}}e^{\eta^{\text{jet2}}}}{2yE_{\text{e}}} \approx x_{\gamma}$
- Sensitivity to process type



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- Sensitivity to process type
- At high- $x_{\gamma}^{\rm obs}$ direct processes dominate



Comparison to ZEUS data for charged hadrons ($N_{ch} > 20$)

Pseudorapidity

- Data well reproduced
- Not sensitive to MPI modelling $(p_{T,0})$



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Multiplicity

- Sensitivity to MPI parameters, clear support for MPIs
- Data within $p_{T,0}$ variations
- Good baseline to study γ +A in UPCs



Comparison to ZEUS data for charged hadrons ($N_{ch} > 20$)

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Multiplicity

- Sensitivity to MPI parameters, clear support for MPIs
- Data within $p_{T,0}$ variations
- Good baseline to study γ +A in UPCs
- Direct contribution negligible in high-multiplicity events (N_{ch} > 20)
 ⇒ Focus on resolved processes



Photon fluxes in Pythia 8

Photon fluxes from Equivalent Photon Approximation (EPA)

• In case of a point-like lepton we have (neglecting electron mass)

$$f_{\gamma}^{l}(x,Q^{2}) = rac{lpha_{em}}{2\pi} rac{1}{Q^{2}} rac{(1+(1-x)^{2})}{x}$$

• For protons need to include form factors, using dipole form factor

$$f_{\gamma}^{p}(x,Q^{2}) = \frac{\alpha_{\text{em}}}{2\pi} \frac{x}{Q^{2}} \frac{1}{(1+Q^{2}/Q_{0}^{2})^{4}} \left[\frac{2(1+\mu_{\text{p}}\tau)}{1+\tau} \left(\frac{1-x}{x^{2}} - \frac{M_{\text{p}}^{2}}{Q^{2}} \right) + \mu_{\text{p}}^{2} \right]$$

where $\tau = Q^2/4M_p^2$, $\mu_p = 2.79$, $Q_0^2 = 0.71 \text{ GeV}^2$

• Drees-Zeppenfeld approximation ($M_p = 0, \mu_p = 1$)

$$f_{\gamma}^{p}(x,Q^{2}) = \frac{\alpha_{em}}{2\pi} \frac{1}{Q^{2}} \frac{1}{(1+Q^{2}/Q_{0}^{2})^{4}} \frac{(1+(1-x)^{2})}{x}$$

- \Rightarrow Large Q^2 suppressed wrt. leptons \Rightarrow photoproduction
 - In ME generators (such as MG5) integrated over Q² and assumed collinear

Define your own photon flux for PYTHIA 8

• Derive a new object from PDF class

class Proton2gammaEPA : public PDF { public: // Constructor. Proton2gammaEPA(int idBeamIn) : PDF(idBeamIn) {} // Update the photon flux. void xfUpdate(int , double x, double Q2) { double mup2 = pow2(20.938); double mup2 = pow2(20.938); double mup2 = pow2(20.938); double fQ4 = 1. / pow4(1 + Q2 / Q20); double fQ4 = 1. / pow4(1 + Q2 / Q20); double tou = Q2 / (4. * m2proton); xgamma = coupling * (pow2(x) / Q2) * (2. * (1. + mup2*tau) / (1. + tau) * ((1 - x)/pow2(x) - m2proton / Q2) + mup2); };

• Pass as a pointer to PYTHIA

pythia.readString("PDF:beamA2gamma = on"); pythia.readString("PDF:beamB2gamma = on"); pythia.readString("PDF:proton2gammaSet = 0"); PDFPtr photonFluxA = make_shared<Proton2gammaEPA>(2212); PDFPtr photonFluxB = make_shared<Proton2gammaEPA>(2212); pythia.setPhotonFluxPtr(photonFluxA, photonFluxB);

Example in p-p: $\gamma \gamma \rightarrow \mu^+ \mu^-$



No finite-size effects
 accounted

Ultraperipheral heavy-ion collisions

- Large impact parameter $(b \gtrsim 2R_A)$ \Rightarrow No strong interactions
- Large flux due to large EM charge of nuclei
- $\Rightarrow \gamma \gamma$ and γA collisions



• With heavy nuclei use *b*-integrated point-like-charge flux

$$f_{\gamma}^{A}(x) = \frac{2\alpha_{\rm EM}Z^{2}}{x\pi} \left[\xi \, K_{1}(\xi) K_{0}(\xi) - \frac{\xi^{2}}{2} \left(K_{1}^{2}(\xi) - K_{0}^{2}(\xi) \right) \right]$$

where $\xi = b_{\min} x m$ where b_{\min} reject nuclear overlap, $Q^2 \ll 1 \text{ GeV}^2$

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Dijets in ultra-peripheral heavy-ion collisions

- Pythia setup with nucleon target only
 ⇒ Not a realistic background for jet reconstruction
- Good agreement out of the box when accounting both direct and resolved
- Also EM nuclear break-up significant





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Photon-ion collisions

Modelling $\gamma\text{-}A$ with Pythia

[by Marius Utheim]

Aim to simulate high-multiplicity events

- Dominated by resolved photons
- ⇒ Set up an explicit VMD model with linear combination of vector-meson states (ρ , ω , ϕ and J/ψ)
 - Use VM PDFs from SU21

[Sjöstrand, Utheim; Eur.Phys.J.C 82 (2022) 1, 21]

• Cross sections from SaS

[Schuler, Sjöstrand; Phys.Rev.D 49 (1994) 2257-2267]

- Sample collision energy from flux
- ⇒ VMD-nucleon scatterings



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Cross sections from SaS

[Schuler, Sjöstrand; Phys.Rev.D 49 (1994) 2257-2267]

- Sample collision energy from flux
- \Rightarrow VMD-nucleon scatterings
 - In line with the full photoproduction



Modelling $\gamma\text{-}A$ with Pythia

[by Marius Utheim]

Angantyr model for heavy ions in Pythia

[Bierlich, Gustafson, Lönnblad, Shah; JHEP 10 (2018) 134]

- Monte Carlo Glauber to sample nucleon configurations
- Cross section fluctuations, fitted to
 partial nucleon-nucleon cross sections
- Secondary (wounded) collisions as diffractive excitations
- Can now handle generic hadron-ion and varying energy [I.H., Utheim; in progress]
- ⇒ VMD-nucleus scatterings





- ATLAS data not corrected for efficiency, estimated with $N_{ch}^{rec} \approx 0.8 \cdot N_{ch}$
- Relative increase in multiplicity well in line with the VMD-Pb setup



- Multiplicity cut adjusted according to the limited efficiency
- Good description of the measured rapidity distribution with the VMD-Pb setup

Two-particle correlations in ATLAS analysis

- ATLAS apply template-fitting method to extract v_n from two-particle correlations
 - Perform a Fourier fit to obtain c_n's for low-multiplicity events (nonflow?)

$$Y^{LM}(\Delta\phi) = c_0 + 2 \cdot \sum_{n=1}^{4} c_n \cos(n\Delta\phi)$$

• Fit high multiplicity $v_{n,n}$'s on top

$$Y^{\text{HM}}(\Delta\phi) = F \cdot Y^{\text{LM}}(\Delta\phi) + G\left[1 + 2 \cdot \sum_{n=2}^{4} v_{n,n} \cos(n\Delta\phi)\right]$$

Free parameters c_n , $v_{n,n}$, F, G

• Can now repeat the fit with Pythia results



Template fit to Pythia simulations



Comparison to ATLAS v_n data



- Simulated results in line with the direct Fourier fit for v_{2,2}
- · Consistent with zero after template fitting (non-flow subraction)
- String interactions in high-multiplicity hadronization, hadronic rescattering?

Summary & Outlook

Summary

- In e+p validated setup for photoproduction at HERA
- Includes fluxes relevant for proton and heavy-ion UPCs
- First steps for full γ +A (8.311)
- \Rightarrow In line with multiplicity distributions
- \Rightarrow As such not consistent with finite v₂

Outlook

- Include full photon structure
- Study different string-interaction effects for high-multiplicity events



[figure by P. Skands]

Backup slides

Рүтны Collaboration

- Christian Bierlich
- Naomi Cooke
- Nishita Desai
- Leif Gellersen
- Ilkka Helenius
- Philip Ilten
- Leif Lönnblad
- Stephen Mrenna
- Christian Preuss
- Torbjörn Sjöstrand
- Peter Skands
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[Pythia meeting in Monash 2019]

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[Pythia meeting in Monash 2019]

- Spokesperson
- Codemaster
- Webmaster

https://pythia.org authors@pythia.org

DGLAP equation for photons

- Additional term due to $\gamma
ightarrow {
m q} \overline{
m q}$ splittings

$$\frac{\partial f_i^{\gamma}(x,Q^2)}{\partial \log(Q^2)} = \frac{\alpha_{\text{em}}}{2\pi} e_i^2 P_{i\gamma}(x) + \frac{\alpha_{\text{s}}(Q^2)}{2\pi} \sum_j \int_x^1 \frac{\mathrm{d}z}{z} P_{ij}(z) f_j(x/z,Q^2)$$

where $P_{i\gamma}(x) = 3(x^2 + (1 - x)^2)$ for quarks, 0 for gluons (LO)

• Resulting PDFs has point-like (or anomalous) and hadron-like components

$$f_i^{\gamma}(x,Q^2) = f_i^{\gamma,\mathsf{pl}}(x,Q^2) + f_i^{\gamma,\mathsf{had}}(x,Q^2)$$

• $f_i^{\gamma, \text{pl}}$: Calculable from perturbative QCD

• $f_i^{\gamma,had}$: Requires non-perturbative input fixed in a global analysis

Photon structure at $Q^2 \sim 0 \text{ GeV}^2$





Linear combination of three components

$$|\gamma\rangle = c_{\rm dir}|\gamma_{\rm dir}\rangle + \sum_{q} c_{q}|q\overline{q}\rangle + \sum_{V} c_{V}|V\rangle$$

where the last term includes a linear combination of vector meson states up to J/ Ψ

$$c_V = \frac{4\pi\alpha_{\rm EM}}{f_V^2}$$

V	$f_V^2/(4\pi)$
$ ho^0$	2.20
ω	23.6
ϕ	18.4
J/Ψ	11.5

Equivalent photon approximation

Compare to full calculation

- Example process $pp \to \gamma\gamma \to \mu^+\mu^-$
- Different approximations (e.g.) by Drees and Zeppenfeld \sim 20% difference to full calculation
- Keeping finite mass and correct magnetic moment provides \sim few percent accuracy
- Not checked for other observables, such as acoplanarity



• Enable γ +p in e+p

pythia.readString("Beams:idA = -11"); pythia.readString("Beams:idB = 2212"); pythia.readString("PDF:beamA2gamma = on");



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pythia.readString("Beams:idA = -11");
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• Enable γ +p in p+p

pythia.readString("Beams:idA = 2212");
pythia.readString("Beams:idB = 2212");
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pythia.readString("Beams:idA = 2212");
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• Enable γ +p in Pb+p

pythia.readString("Beams:idA = 2212"); pythia.readString("PDF:beamA2gamma = on"); pythia.readString("PDF:beamA2gammaSet = 0"); pythia.readString("PDF:beam2gammaApprox = 2"); pythia.readString("Photon:sample02 = off"); PDFPtr photonFlux = make_shared<Nucleus2gamma>(2212); pythia.setPhotonFluxPtr(photonFlux, 0);



For more examples see main68.cc, main69.cc, main70.cc, main78.cc in examples directory



class Nucleus2gamma2 : public PDF { public: Nucleus2aamma2(int idBeamIn) : PDF(idBeamIn) {} void xfUpdate(int , double x, double) { double bmin = 2 * 6.636: double z = 82.: double $m^2 = pow^2(0.9314)$: double alphaEM = 0.007297353080; double hbarc = 0.197: double xi = x * sart(m2) * bmin / hbarc:double bK0 = besselK0(xi); double bK1 = besselK1(xi): double intB = xi * bK1 * bK0 - 0.5 * pow2(xi) * (pow2(bK1) - pow2(bK0)) xaamma = 2. * alphaEM * pow2(z) / M PI * intB:

[from main70.cc]



An example process: $\gamma\gamma \to \mu^+\mu^-$

- Can take place in EE, SD and DD (also DY processes with resolved photons?)
- Implemented natively in Pythia, can also generate with an ME generator (MG5, SC)

EE contribution

- Clean process to study fluxes
- However, fluxes only does not account for finite-size effects



[ATLAS: PLB 777 (2018) 303-323]

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- Implemented natively in Pythia, can also generate with an ME generator (MG5, SC)

EE contribution

- Clean process to study fluxes
- However, fluxes only does not account for finite-size effects
- Not quite back-to-back due to
 - p_T generated by non-collinear photons
 - QED radiation in the final state
- Acoplanarity $|\pi-\Delta\phi|$ quantify the effect



- Needed to tune Pythia primordial k_T parameters for external events
- Can use (user-defined) flux for Q² sampling

Heavy-ion collisions

• Angantyr in Pythia provides a full heavy-ion collisions framework

[Bierlich, Gustafson, Lönnblad & Shah: 1806.10820]

· Hadronic rescattering can be included as well, enhances collective effects

[CB, Ferreres-Solé, Sjöstrand & Utheim: 1808.04619, 2005.05658, 2103.09665]





p+A collisions

[Bierlich, Gustafson, Lönnblad & Shah: 1806.10820]

- Angantyr can be applied also to asymmetric p+A collisions
- The centrality measure well reproduced
- · Similarly centraility-dependent multiplicities



ATLAS data for v_n in γ +Pb



- Non-zero flow coefficients also for γ +Pb
- Expected baseline from MC simulations?



- Pythia8 γ +p in ATLAS result should correspond to gm-p on right
- Relative increase in multiplicity well in line with the VMD setup



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- Relative shift in rapidity distribution in line with the VMD setup using Angantyr



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- $\Sigma_{\gamma} \Delta \eta$: Sum of rapidity gaps for which $\Delta \eta > 0.5$
- Similar for γ -p and γ -Pb

Role of cross section fluctuations



 High-multiplicity tail less pronounced with Angantyr:CollisionModel = 0 with fixed nucleon radius, ATLAS data seem to favour fluctuations

Energy distributions vs. multiplicity

