## **Thermodynamical String Fragmentation**

with Torbjörn Sjöstrand - arXiv:1610.09818

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MCnet







## Motivation



#### $p_{\perp}$ distributions (ratio plots)



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#### Enhanced strangeness with increasing $n_{ch}$



Elayour and transverse momentum of hadrons:

- string streched between qq
- $q\bar{q}$  moves apart  $\rightarrow$  energy stored in string (potential  $V(r) = \kappa r$ )
- creation of  $q_i \bar{q}_i$  pairs breaks string:

 $m_{\perp q_i} = 0$  on-shell production in single vertex

 $m_{\perp q_i} > 0$  tunneling probability

$$q_3\bar{q}$$
  $q_2\bar{q}_3$   $q_1\bar{q}_2$   $qq_1$   
 $q_2\bar{q}_3$   $q_1\bar{q}_2$   
 $q_2\bar{q}_3$   $q_1\bar{q}_2$   
 $q_1\bar{q}_2$   $q_1\bar{q}_2$   
 $q_1\bar{q}_2$   $q_1\bar{q}_2$   $q_1\bar{q}_2$   
 $q_1\bar{q}_2$   $q_1\bar{q}_2$ 

$$\begin{split} \exp\left(-\pi \, m_{\perp\,\mathbf{q}_{i}}^{2}/\kappa\right) &= \exp\left(-\pi \, m_{\mathbf{q}_{i}}^{2}/\kappa\right) \exp\left(-\pi \, p_{\perp\,\mathbf{q}_{i}}^{2}/\kappa\right) \\ &\downarrow \qquad \qquad \downarrow \\ \text{flavour selection of } \mathbf{q}_{i}\bar{\mathbf{q}}_{i} \qquad \qquad \langle p_{\perp\,\mathbf{q}_{i}}^{2}\rangle &= \kappa/\pi = \sigma^{2} \end{split}$$

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• lots of flavour parameters: - suppression of strangeness and diquarks,  $\eta$  and  $\eta'$ 

- rates for different meson multiplets

O(20) free parameters in total

Idea: hadron-level suppression

$$\exp{(-m_{\perp}\,{\rm had}/T)}$$
 with  $m_{\perp}\,{\rm had}=\sqrt{m_{\rm had}^2+p_{\perp}^2\,{\rm had}}$ 

• generate  $p_{\perp \text{ had}}$  according to

 $f_{\rm had}(p_{\perp\,{\rm had}})\,{\rm d}\,p_{\perp\,{\rm had}} = \exp\left(-p_{\perp\,{\rm had}}/T\right)\,{\rm d}\,p_{\perp\,{\rm had}}$ 

• fourier transformation to obtain quark-level distribution

$$f_{\mathsf{q}}(p_{\perp\,\mathsf{q}}) \propto \int_{0}^{\infty} \frac{b J_{0}(b \, p_{\perp\,\mathsf{q}}/T)}{(1+b^{2})^{3/4}} \mathsf{d} \, b \qquad \left[ \text{ fit: } \mathcal{N} \; \frac{\exp(-c \, p_{\perp\,\mathsf{q}}/T)}{(p_{\perp\,\mathsf{q}}/T)^{d}} \right]$$

- pick hadron flavour according to  $P_{\text{had}} = \exp\left(-m_{\perp \text{had}}/T\right)$ 

+ multiplicative factors for spin-counting, SU(6) symmetry factors, ...

- heavier hadrons obtain more  $p_{\perp}$
- 3 free parameters in total





Idea: more MPIs  $\Rightarrow$  closer packing of strings

- transverse region shrinks  $\Rightarrow$  larger string tension
- guess momentum of next hadron, based on average quantities
- $n_{\text{string}}$  = number of strings that cross hadron rapidity
- effective number of strings  $n_{\text{string}}^{\text{eff}} = 1 + \frac{n_{\text{string}} 1}{1 + p_{\perp \text{ had}}^2 / p_{\perp 0}^2}$
- modify Gaussian width  $\sigma \rightarrow \left(n_{\mathrm{string}}^{\mathrm{eff}}\right)^r \sigma$  (similar for temperature)



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## Hadron Rescattering

Idea: dense hadronic gas  $\Rightarrow$  hadrons might rescatter on the way out

Find hadron pairs that can scatter:

- cut on the invariant mass of the hadron pair
- rescattering probability: overall probability

- in CoM frame rotate around angles chosen flat in d  $\Omega$ 





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Pds

P<sub>ds</sub><sup>ma</sup>









#### Transverse momentum distributions: inclusive and pions





#### Transverse momentum distributions: protons and kaons





#### Enhanced strangeness with increasing $n_{ch}$



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What is new?

- option for generating  $p_{\perp had}$  according to  $\exp(-p_{\perp had}/T)$  with flavour selection according to  $\exp(-m_{\perp had}/T)$
- effect of close-packing of strings
- simple model for hadron rescattering

What does it do?

- improves some observables, such as  $p_{\perp}$  spectra,  $\langle p_{\perp} \rangle (m_{\rm had})$
- does not improve everything, e.g. kaon  $p_{\perp}$  remains difficult
- hadron decays are a limiting factor



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Further work required!

- microscopic tracing of the full space-time evolution (partons and hadrons, production and decay vertices)
- more detailed understanding and modelling



# Backup



Toy model with d and s quarks only

- (d ightarrow s) competes with (d ightarrow d) ightarrow ds obtains larger  $p_{\perp}$
- $(s \rightarrow d)$  competes with  $(s \rightarrow s) \rightarrow s\bar{d}$  obtains smaller  $p_{\perp}$



## **Rapidity Distributions**





## Limiting factor: Decays



#### pion transverse momentum @ LHC, with and without decays, similar for protons



 $\Rightarrow$  decays wash out effects present after fragmentation



 $\langle p_{\perp} \rangle$  in toy model (5 strings with  $E = m_Z$  on the z axis)





#### Average transverse momentum: as a function of $n_{ch}$ and $m_{had}$

